Operator algebras: C*-algebras and groupoids

Operátorové algebry a C*-algebry příslušné grupoidům NMMA652

Wednesdays, 13:30-15:00

Institute of Mathematics, Czech Academy of Sciences Žitná 25, ground floor seminar room, back building

Course instructors: Karen Strung (<u>strung.me</u>) and Tristan Bice (<u>sites.google.com/site/tristanbice/</u>)

This course pairs well with NMAG583: Noncommutative Geometry and Topology Seminar (Tuesdays 16:00, Žitná 25 and Zoom) ncgandtprague.wordpress.com/ncgt-seminar/

NMMA652

Wednesdays 13:30 to 15:00 at IMCAS and on Zoom

For more information, please contact Karen Strung strung@math.cas.cz

The study of C*-algebras fits into the broader framework of operator algebras. Operator algebras were introduced by Murray and von Neumann to model noncommutative behaviour observed in **quantum physics**.

C*-algebras lie at the intersection of algebra, topology, and analysis. They are an active and exciting area of research.

This course will begin with the basic theory of C*-algebras, including the Gelfand theorem which establishes C*-algebras as "noncommutative topological spaces", representation theory and the Gelfand–Naimark theorem, as well as other basic structural properties.

The second part of the course will focus on C*-algebras which are constructed by **topological groupoids**—objects generalizing **groups** which can be defined in terms of **category theory**. Groupoid C*-algebras are encompass many types of C*-algebras, including group C*-algebras and crossed products.

We will see how the underlying groupoid informs the structure of the C*-algebra, and vice versa.

Student evaluation will be based on a short talk on a relevant topic of their choice.